

“Reply to Discussion of Analysis of the internal stability of granular soils using different methods”

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1 **Introduction**

2 The authors wish to thank the discussers for the interesting
3 comments that allowed us to deepen further the published
4 paper. The method proposed by the authors (Moraci et al.
5 2014) summarizes the generally used criteria to evaluate the
6 internal stability of cohesionless sand-gravel soils (i.e. Kezdi,
7 1969; Sherard, 1979; and Kenney and Lau, 1985 and 1986).
8 The results of the method proposed by the authors are
9 obtained as the average of Sherard (1979) and Kenney and
10 Lau (1985 and 1986) methods. Therefore, the authors' method
11 results are conservative for soils for which both the used
12 methods provide conservative results. Kezdi's criterion has not
13 been considered in the reply because it is similar to Sherard's
14 criterion and it is more conservative than the Sherard's one.

15

16 **About the grain size distributions of soils analyzed by Ni**
17 **et al. (2014)**

18 The soils analyzed in the discussion by Ni et al. (2014) are silt
19 sand-gravel and clay-silt-sand-gravel soils. Some of the soils
20 reported in Figures 1 and 2, show many potential zones of

21 instability, in contrast with those considered by Moraci et al.
22 (2014) in the published paper. For these soils the evaluation of
23 S and F is complex and requires a more detailed explanation.
24 Therefore, in order to apply the method to all the cohesionless
25 soils, in the following paragraphs it will be explained how
26 evaluating F and S considering that the choice of the values
27 depends on the shape of the grain size distribution.

28 **About the choice of F**

29 The research topic of the Moraci et al. (2014) paper is the
30 study of fine particles suffusion inside the solid skeleton
31 constituted by coarse particles. Therefore, according to
32 Skempton and Brogan (1994), the maximum value considered
33 for the fine fraction in weight (F) has been 35%. This value has
34 been chosen because, for fine fraction larger than 35%, the
35 coarse particles do not belong to the solid skeleton but they
36 are immersed in a matrix constituted by the fine particles. For
37 this reason, for the analysis of the soil 11/WF, studied by the
38 discussor, the authors suggest to use other methods such as
39 the one proposed by Moraci et al. (2012a).

40 In the proposed method the F value is evaluated as the mean
41 value between F1, evaluated by means of Kenney and Lau's
42 method, and F2, evaluated by means of Sherard's method.

43 ***Evaluation of F1***

44 The value of F1 is determined, in the range of finer percentage
45 (F) from 0% to 35%, corresponding to the minimum value of
46 (H/F) obtained by the graph H/F vs. F (Figg. 3b-d, 4b-d, 5b-d,
47 6b-d, 7b-d).

48 ***Evaluation of F2***

49 F2 is generally determined corresponding to the absolute or
50 relative maximum value of I_r nearby to maximum theoretical
51 limit value for which the fine particles suffusion, inside the solid
52 skeleton constituted by coarse particles, occurs, assumed
53 according to Skempton and Brogan (1994) equal to 35%
54 (Figg. 4c and 7c).

55 If the I_r vs. F is a decreasing monotonic curve and it intercepts
56 the limit line of internal stability index, $I_r=5$, F2 is taken at the
57 intersection with the limit line (Figg. 3c and 6c).

58 On the other hand, if the I_r vs. F is a decreasing monotonic
59 curve and it is located below the limit line ($I_r=5$), Fig. 5c, F_2 is
60 equal to 0, corresponding to the maximum value of I_r .

61 **About the choice of S**

62 Once the values of F_1 and F_2 have been evaluated, the S
63 value is evaluated as average between S_1 and S_2 ,
64 determined on the S versus F curves respectively according to
65 Kenney and Lau method (for F_1) and according to Sherard
66 method (F_2), as follows:

$$67 \quad S = \frac{[S_1 + S_2]}{2} \quad (1)$$

68 In the following, it is explained how the curves S vs. F are
69 determined according to the two different methods.

70 According to Kenney and Lau method, the S versus F curve is
71 evaluated, for each diameter (D_a) of the soil grain size
72 distribution, as the secant slope in the range from D_a to $4D_a$,
73 as follows (Fig. 8):

$$74 \quad S(F_a) = \frac{Y_e - Y_a}{X_e - X_a} = \frac{F_e - F_a}{\log 4D_a - \log D_a} = \frac{F_e - F_a}{\log 4} \quad (2)$$

75 According to Sherard method, the S versus F curve is
76 determined, for each diameter (D_a) of the soil grain size
77 distribution, as the secant slope, as follows (Fig. 8):

$$78 \quad S(F_a) = \frac{Y_c - Y_b}{X_c - X_b} = \frac{F_c - F_b}{\log D_c - \log D_b} = \frac{0.15}{\log \frac{D_c}{D_b}} \quad (3)$$

79 Where:

80 the point A corresponds to $Y_a = F_a$ and $X_a = \log D_a$;

81 the Point B corresponds to $Y_b = F_b = 0.85F_a$ and $X_b = \log D_b$;

82 the Point C corresponds to $Y_c = F_c = Y_b + 0.15 = 0.85F_a + 0.15$ and
83 $X_c = \log D_c$.

84 For example the determination of S1 and S2 for some soils
85 analyzed by the discussor are shown, respectively, in Figures
86 3f, 4f, 5f, 6f, 7f (for S1) and in Figures 3e, 4e, 5e, 6e, 7e (for
87 S2).

88

89 **Analysis of soils studied by Ni et al. (2014) using the**
90 **method proposed by the authors (“butterfly wings” chart**
91 **method)**

92 The soils studied by Ni et al. (2014) have been analyzed
93 according to the selection criteria of F and S, as previously
94 illustrated, and the results are shown in the “butterfly wings”

95 chart proposed by the authors (Fig. 9). In the chart, the Kezdi's
96 criterion has not been shown because it is similar to the
97 Sherard's criterion and it is more conservative than the
98 Sherard's one.

99 The comparison between the results obtained using the
100 method proposed by Moraci et al. (2014) and the experimental
101 results obtained, using different laboratory procedures, by
102 Kenney and Lau (1985), Skempton and Brogan (1994), Wan
103 and Fell (2004) and Sadaghiani and Witt (2011), is
104 summarized in Table 1.

105 The figure 9 shows that the soils 23/KL, 21/KL, 20/KL, 1/KL,
106 2/KL, 3/KL, As/KL and C/SB fall in the stable zone of "butterfly
107 wings" according to the different experimental results.

108 The soils Ds/KL, D/SB, Ys/KL, B/SB, fall in the uncertain zone
109 A; these soils according to the different experimental tests
110 result stable (Ds/KL, D/SB) or unstable (Ys/KL, B/SB).

111 The soils 3R/WF and A/KL fall in uncertain zone B; the soil
112 4R/WF falls to the border line between the unstable zone and
113 uncertain zone B. According to the different experimental

114 results, the soils 3R/WF and 4R/WF result stable while the soil
115 A/KL results unstable.

116 The soils Y/KL, X/KL, RD/WF, 1,1A/WF, 2R/WF, A3/WF,
117 9/WF, SOIL/SW, B1/WF, B2/WF, D1/WF, C1/WF, A2/WF,
118 10/WF, fall in the unstable zone. Almost all these soils result
119 unstable according to the different experimental results; only
120 the soils RD/WF, 9/WF, 1,1A/WF and 2R/WF result
121 experimentally stable.

122 **About the filtration tests**

123 For broadly graded granular soils and especially for silt sand-
124 gravel and clay-silt-sand-gravel soils the experimental results
125 of filtration tests could be affected by different test factors. The
126 first one is related to the difficulty to reconstitute homogeneous
127 soil specimens (generally for these soils in order to obtain
128 homogeneous specimens the slurry deposition technique
129 should be used, Kuerbis and Vaid, 1988). In the case of non-
130 homogeneous specimens, the procedure used by Wan and
131 Fell (2004) to assess the size of the largest particles eroded
132 by suffusion process and the fraction of materials eroded by
133 the process could be approximated.

134 The second one is linked to the fact that the soil subjected to
135 filtration tests is in contact with a gravel layer that, for some
136 soils, could behave as filter and, therefore, could affect the
137 movement of soil particles.

138 Moreover, the results of seepage tests could be affected by
139 the presence of air inside the soil specimens, if deaired water
140 is not used in the tests and the soil specimens have not been
141 saturated.

142 For these soils, for which is really complex to perform proper
143 experimental tests, the authors suggest to use geometric-
144 probabilistic methods, such as the Simulfiltr method proposed
145 by Moraci et al. (2012b, c). These methods are capable to
146 simulate the real soil grain size distribution considering
147 different soil relative density (or porosity) and to simulate the
148 fine particles movement inside the pores of solid skeleton
149 constituted by the coarse particles (regardless of interaction
150 with filter) .

151

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Figure Captions

Fig.1 Stable soils according to experimental results obtained by different authors (Ni et al. 2014).

Fig.2 Unstable soils according to experimental results obtained by different authors (Ni et al. 2014).

Fig.3. Example of evaluation of F and S for soil 3R/WF: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

Fig.4. Example of evaluation of F and S for soil 10/WF: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

Fig.5. Example of evaluation of F and S for soil 23/KL: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

Fig.6. Example of evaluation of F and S for soil Ds/KL: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

Fig.7. Example of evaluation of F and S for soil B1/WF: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

Fig. 8. Example of determination of S (F) according to Kenney and Lau (1985) and Sherard (1979) methods.

Fig. 9. Butterfly wings chart: results obtained for the soils analyzed by Ni et al. (2014).

Insert Figures Here

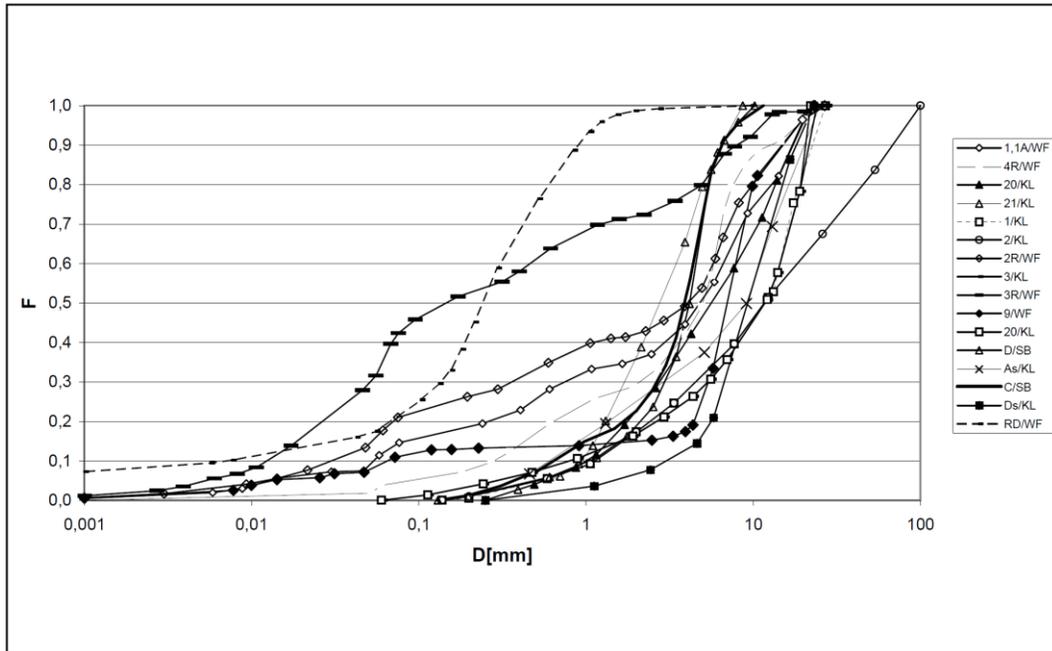


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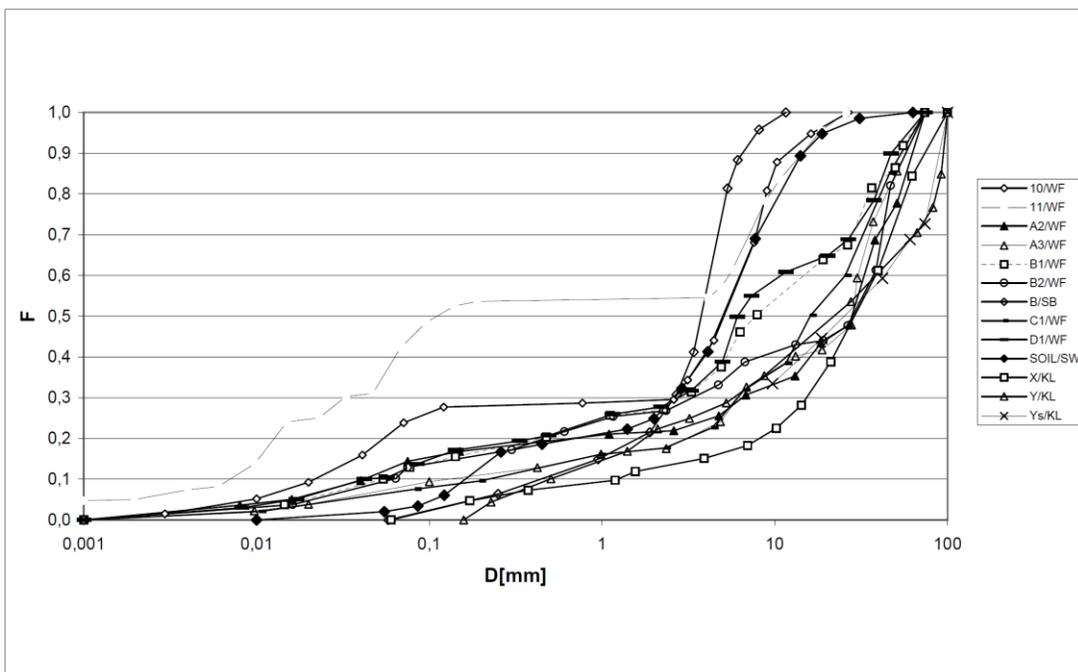


Fig.2 Unstable soils according to experimental results obtained by different authors (Ni et al. 2014).

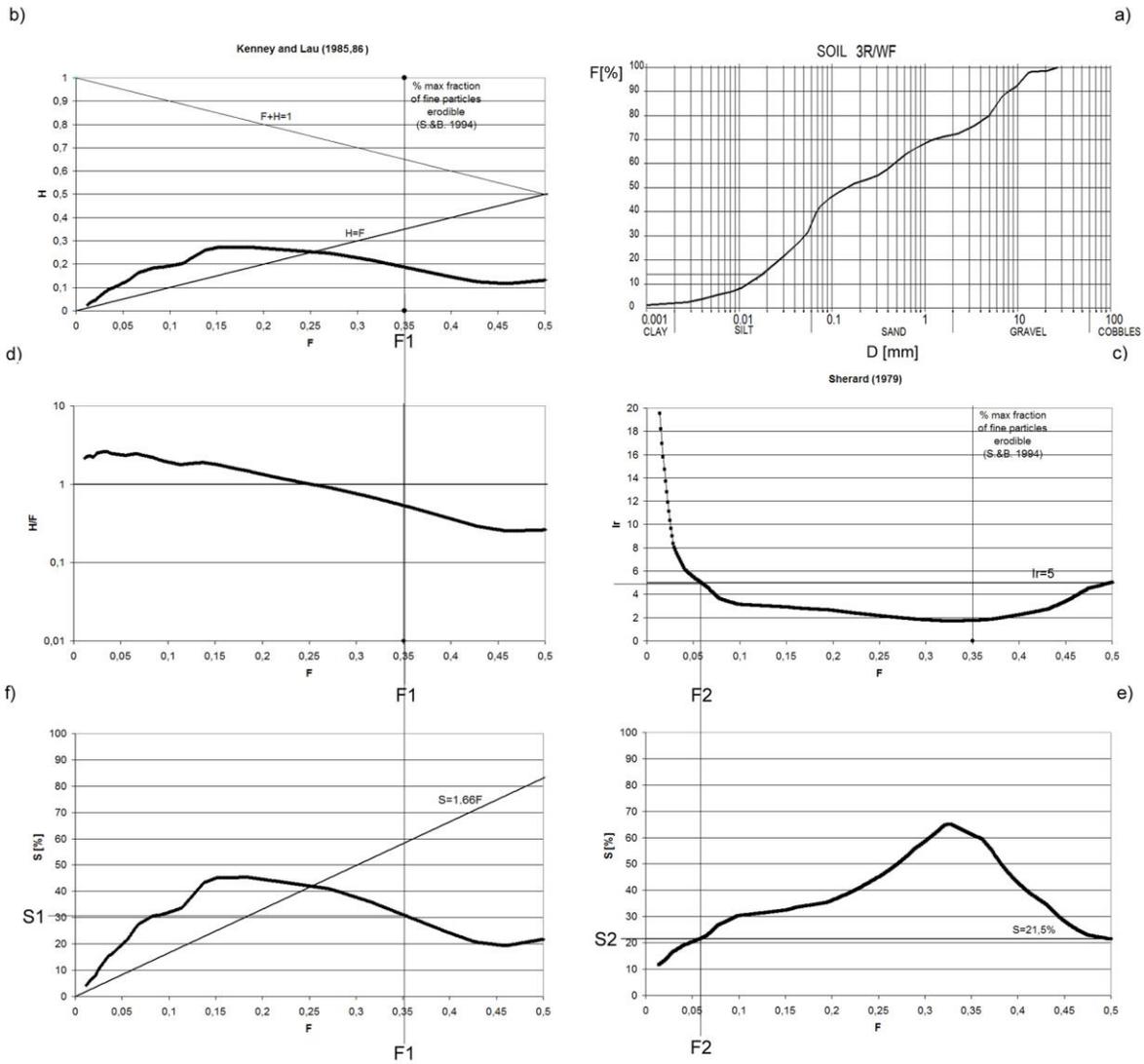


Fig. 3. Example of evaluation of F and S for soil 3R/WF: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) Ir vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

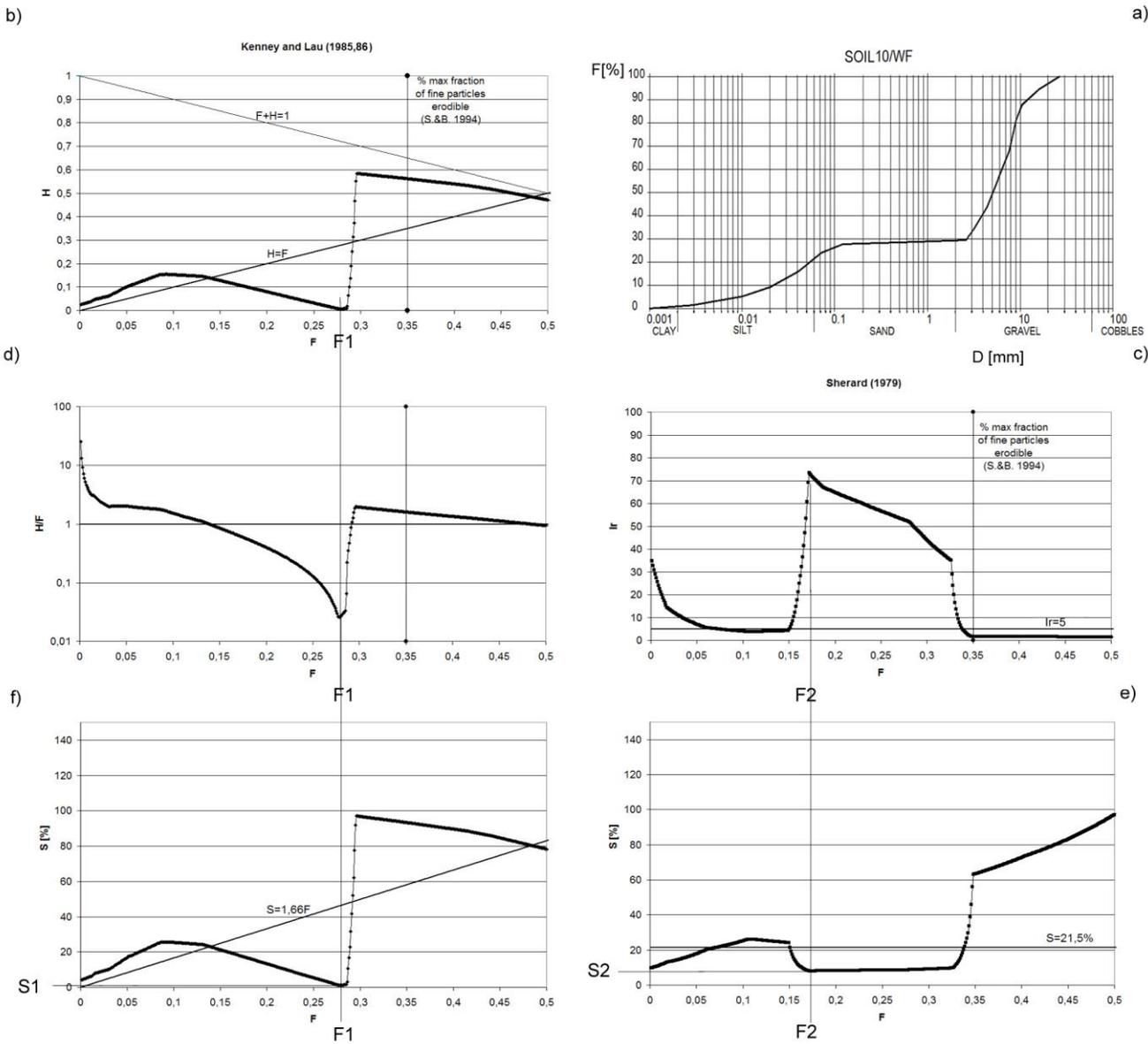


Fig.4. Example of evaluation of F and S for soil 10/WF: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

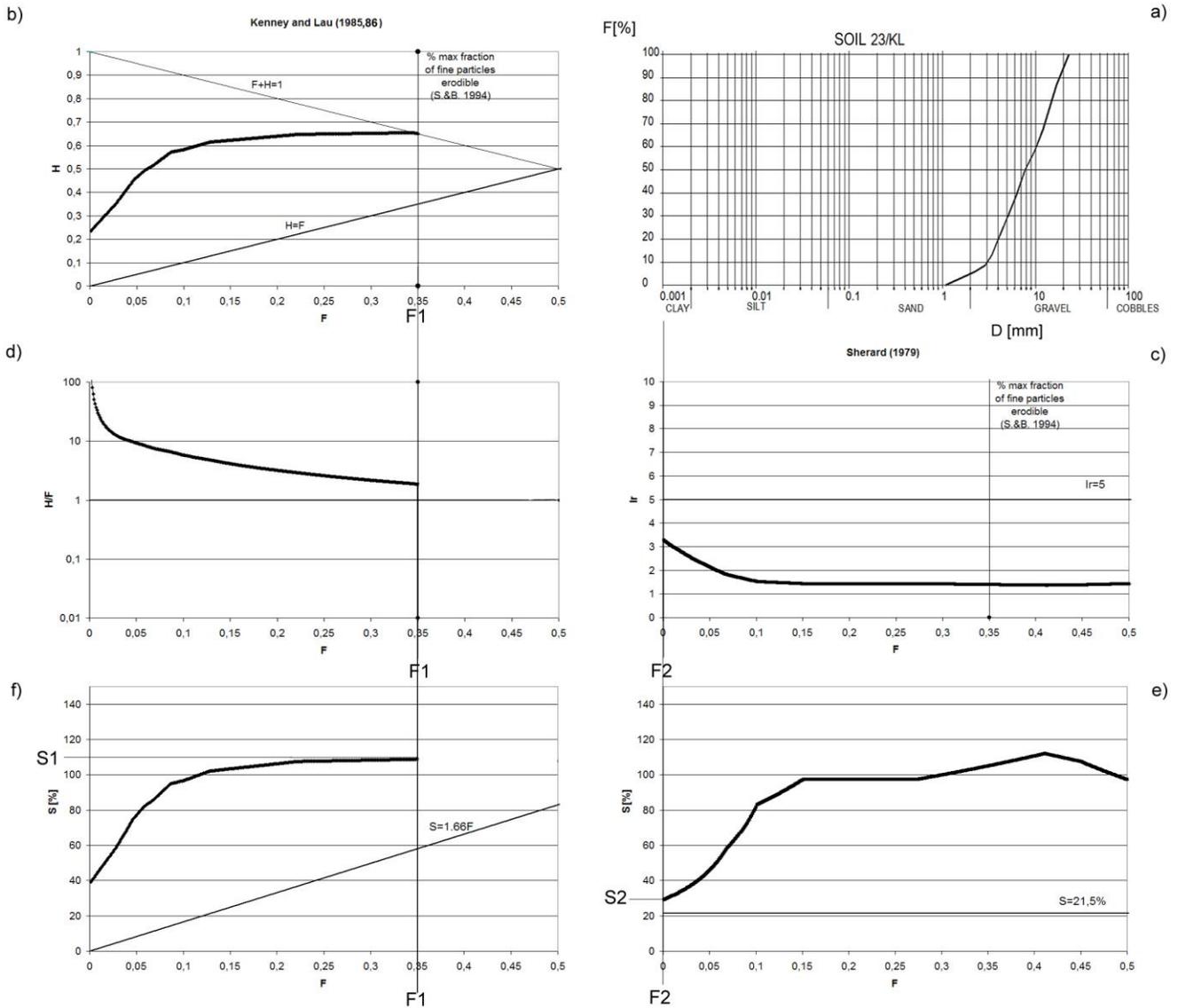


Fig.5. Example of evaluation of F and S for soil 23/KL: a) soil grain size distribution; b) shape curve according to Kenney and Lau (1985 and 1986); c) I_r vs. F curve according to Sherard (1979); d) H/F vs. F curve according to Kenney and Lau (1985); e) S vs. F curve according to Sherard (1979); f) S vs. F curve according to Kenney and Lau (1985).

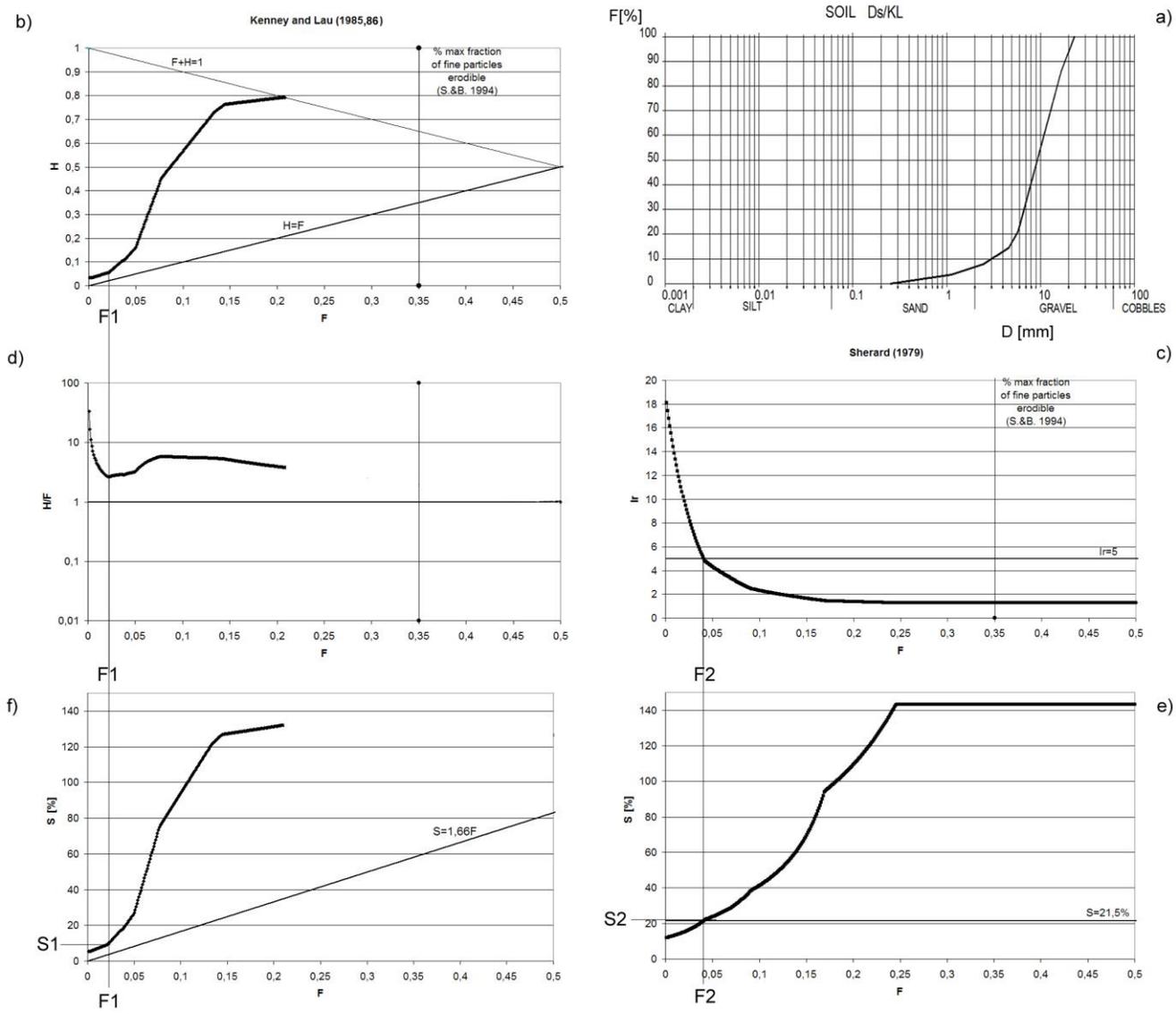


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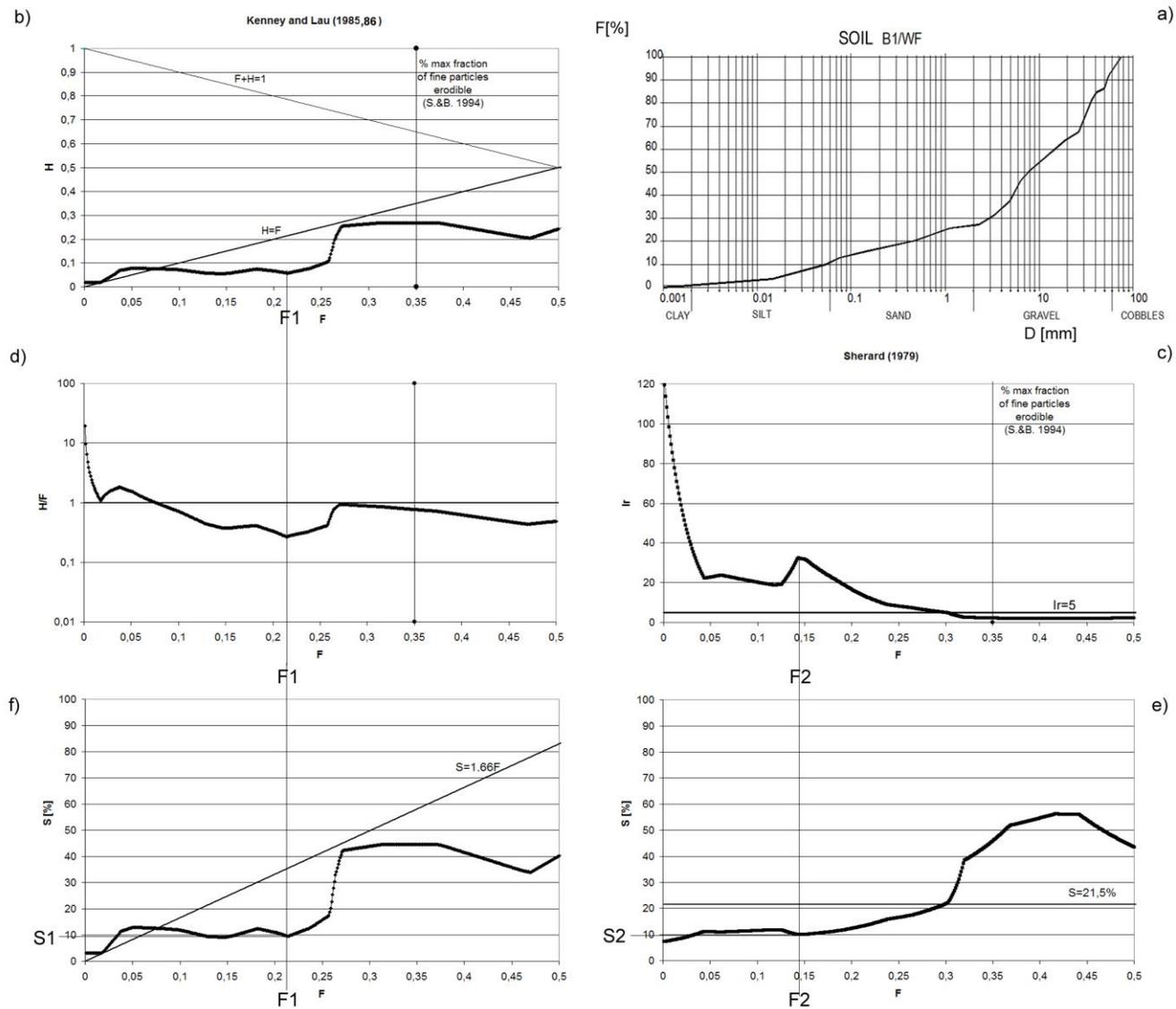


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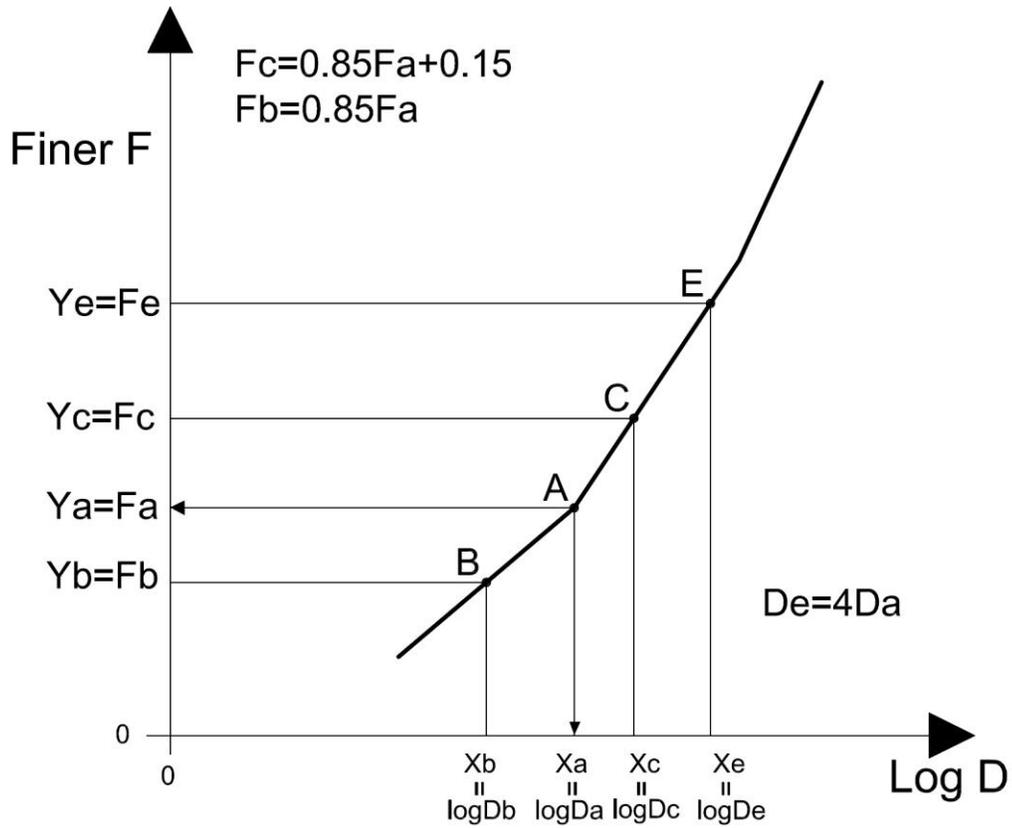


Fig. 8. Example of determination of S (F) according to Kenney and Lau (1985) and Sherard (1979) methods.

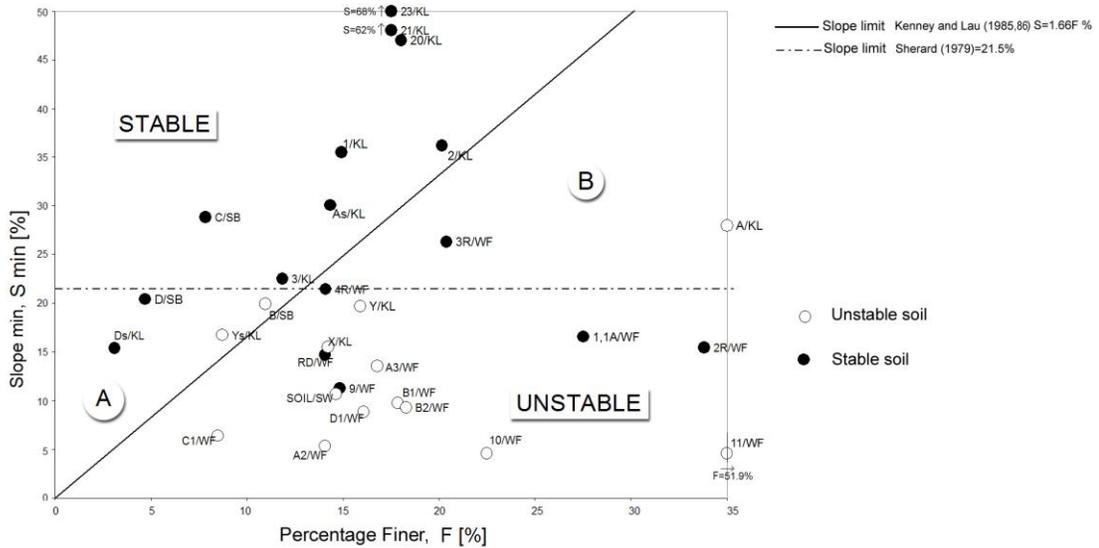


Fig. 9. Butterfly wings chart: results obtained for the soils analyzed by Ni et al. (2014).

Table 1. Comparison between “butterfly wings method” results and experimental results

Soil	Butterfly wings method results	Experimental results according to the different authors
1,1 A	Unstable	Stable (WF)
2R	Unstable	Stable (WF)
10	Unstable	Unstable (WF)
B2	Unstable	Unstable (WF)
B1	Unstable	Unstable (WF)
D1	Unstable	Unstable (WF)
A2	Unstable	Unstable (WF)
C1	Unstable	Unstable (WF)
SOIL	Unstable	Unstable (SW)
9	Unstable	Stable (WF)
11	Unstable *	Unstable (WF)
A3	Unstable	Unstable (WF)
RD	Unstable	Stable (WF)
X	Unstable	Unstable (KL)
Y	Unstable	Unstable (KL)
As	Stable	Stable (KL)
Ys	Uncertain A	Unstable (KL)
B	Uncertain A	Unstable (SB)
Ds	Uncertain A	Stable (KL)
D	Uncertain A	Stable (KL)
4R	Unstable, Uncertain B	Stable (WF)

3R	Uncertain B	Stable (WF)
A	Uncertain B	Unstable (KL)
3	Stable	Stable (KL)
C	Stable	Stable (SB)
1	Stable	Stable (KL)
2	Stable	Stable (KL)
20	Stable	Stable (KL)
21	Stable	Stable (KL)
23	Stable	Stable (KL)

* in the soil 11 the coarser fraction is floating in the finer fraction

WF= Wan and Fell (2004), SW= Sadaghiani and Witt (2011), SB= Skempton and Brogan (1994), KL= Kenney and Lau (1985).